

# Pollution, Public Health Care, and Life Expectancy when Inequality Matters

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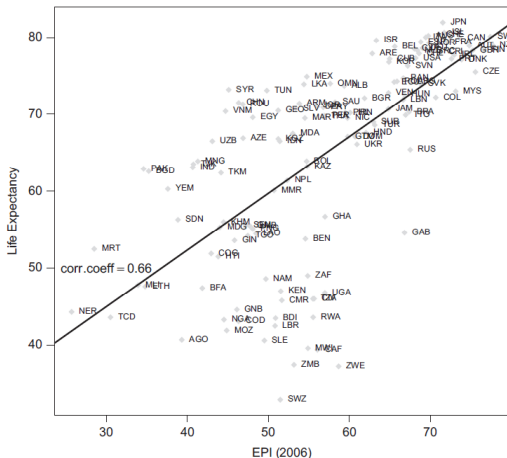
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## Health, Education and Retirement over the Prolonged Life Cycle

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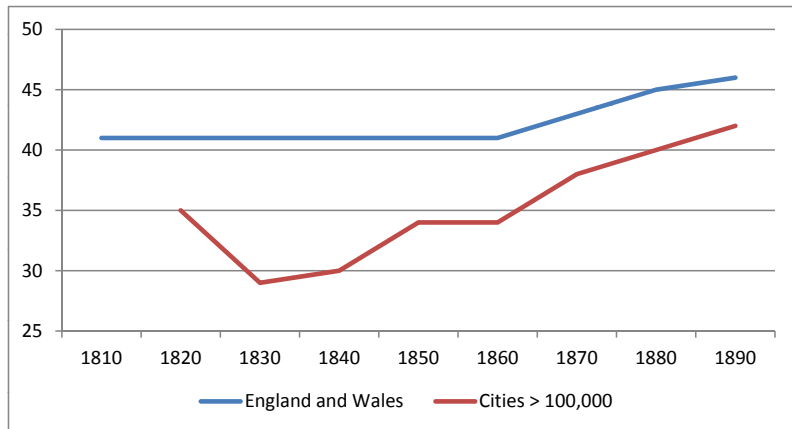
# Introduction

Life expectancy and environmental quality (Mariani, Perez-Barahona, and Natacha Raffin, 2010):



# Introduction

Life expectancy at birth (Szreter, 1997):



- Human capital investments are positively affected by life expectancy
- Life expectancy depends on health expenditures and is adversely affected by the degradation of the environment
- The productivity of health expenditures depends on the level of environmental pollution
- In addition, the distribution of wealth triggers the skill composition of the labor force (Galor and Zeira, 1993)
- Interaction between longevity, pollution and health has been analyzed by Raffin and Segmüller (2012)
- Link between longevity and environmental traps (no policy) by Mariani, Perez-Barahona, and Natacha Raffin (2010)
- We analyze the link between inequality, pollution and life expectancy within a Galor/Zeira framework

# Description of the model

- Small open economy populated by a continuum of overlapping generations
- Agents live for two periods
- In the second period of life, agents derive utility out of consumption and (inter vivo) bequests
- Survival in the second period of life is uncertain
- In their first period of life, agents decide whether or not to invest in skills
- Unskilled households work in both periods while skilled households work in their last period only
- Capital market imperfection with respect to human capital investments
- Production generates income and pollution
- Government collects taxes in order to finance abatement measures and health expenditures

- Production takes place in a skilled and in an unskilled sector  $u, s$ :

$$Y_t^u = aL_t^u, \quad a > 0, \quad (1)$$

$$Y_t^s = b(K_t)^\gamma (L_t^s)^{1-\gamma}, \quad b > 0, \gamma \in (0, 1) \quad (2)$$

- Aggregate output is given by

$$Y_t = Y_t^s + Y_t^u. \quad (3)$$

- SOE assumption implies  $r = \bar{r}$  and a constant  $k_t = K_t/L_t^s$  such that

$$\bar{r} = \gamma b k_t^{\gamma-1} - \delta \Rightarrow Y_t^s = b^{\frac{1}{1-\gamma}} \left( \frac{\gamma}{\bar{r} + \delta} \right)^{\frac{\gamma}{1-\gamma}} L_t^s, \quad (4)$$

and

$$w_t^s = (1 - \gamma) b k_t^\gamma = (1 - \gamma) b^{\frac{1}{1-\gamma}} \left( \frac{\gamma}{\bar{r} + \delta} \right)^{\frac{\gamma}{1-\gamma}}, \quad (5)$$

$$w_t^u = a. \quad (6)$$

- The pollution stock evolves over time according to

$$P_{t+1} = (1 - \eta)P_t + \varepsilon_0 Y_t - \varepsilon_1 A_t, \quad 0 < \varepsilon_1 < \varepsilon_0, \quad \eta \in (0, 1), \quad (7)$$

- Government raises income taxes  $\tau \in (0, 1)$  in order to finance public health expenditures  $H_t$  and abatement measures  $A_t$ .
- Abstracting from intertemporal debts and assuming constant expenditure shares for public health,  $\nu$ , and abatement measures,  $1 - \nu$ , a balanced budget in each period requires

$$H_t = \nu G_t, \quad (8)$$

$$A_t = (1 - \nu)G_t, \quad \nu \in (0, 1). \quad (9)$$

- An individual born in  $t - 1$  expects to live for  $1 + \phi_t$  periods, with  $0 \leq \phi_t \leq 1$
- $\phi_t$  is a non-decreasing function in public health care expenditures,  $H_t$ , and a non-increasing function in the pollution stock  $P_t$ , such that

$$\frac{\partial \phi(H_t, P_t)}{\partial H_t} \geq 0, \quad \frac{\partial \phi(H_t, P_t)}{\partial P_t} \leq 0. \quad (10)$$

Moreover, the cross-derivative is non-positive, i.e.  $\frac{\partial^2 \phi(H_t, P_t)}{\partial H_t \partial P_t} \leq 0$ .

- utility in  $t$  of an agent  $j$  born in  $t - 1$  reads

$$\bar{u}_t^j = \phi_t [\alpha \ln c_t^j + (1 - \alpha) \ln x_t^j] \quad (11)$$

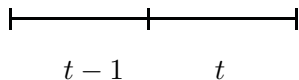
- Given income taxes  $\tau \in (0, 1)$  and lifetime income  $y_t^j$ , we obtain

$$c_t^j = \alpha(1 - \tau)y_t^j, \quad (12)$$

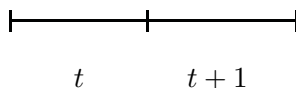
$$x_t^j = (1 - \alpha)(1 - \tau)y_t^j. \quad (13)$$



$$u_t^j = \phi_t \left\{ \overbrace{\alpha \ln c_t^j + (1 - \alpha) \ln x_t^j}^{\bar{\alpha} + \ln[(1 - \tau)y_t^i]} \right\}$$



$$u_{t+1}^j = \phi_{t+1} \left\{ \overbrace{\alpha \ln c_{t+1}^j + (1 - \alpha) \ln x_{t+1}^j}^{\bar{\alpha} + \ln[(1 - \tau)y_{t+1}^i]} \right\}$$



- The credit market is subject to imperfections as in Galor and Zeira (1993)  $\Rightarrow$  borrowers' interest rate,  $i_t$ , exceeds the world market interest rate,  $\bar{r}$ .
- In contrast to Galor and Zeira (1993),  $i_t$  depends inversely on agents' life expectancy,  $\phi_t$ . Moreover,  $i_t$  is not time invariant and affected by public health expenditures and abatement measures

$$i_t = \frac{\beta}{(\beta - 1)} \frac{(1 + \bar{r})}{\phi_t} - 1, \quad \beta > 1. \quad (14)$$

- Since  $\beta > 1$  it follows that  $i_t > \bar{r}$ .
- Moreover,  $\frac{\partial i_t}{\partial \phi_t} < 0$ , such that higher health risks increase lenders' credit costs.

# The evolution of wealth

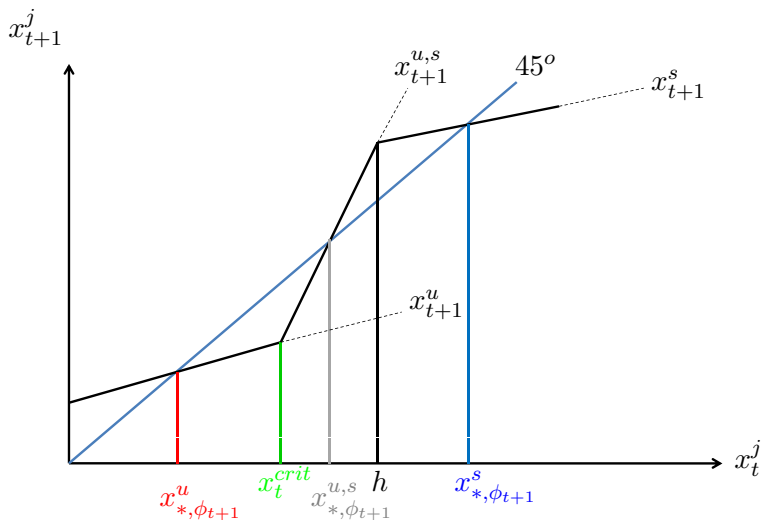
- Whether or not to invest in human capital depends on the level of inherited bequests, i.e.  $x_t^j \gtrless h$ , and life expectancy  $\phi_{t+1}$
- Households with  $x_t^j \geq h$  invest in human capital, if  $u_{t+1}^s \geq u_{t+1}^u$

$$\underbrace{\phi_{t+1}w^s + (x_t^j - h)(1 + \bar{r})}_{y_{t+1}^s} \geq \underbrace{\phi_{t+1}w^u + ((1 - \tau)w^u + x_t^j)(1 + \bar{r})}_{y_{t+1}^u} \quad (15)$$

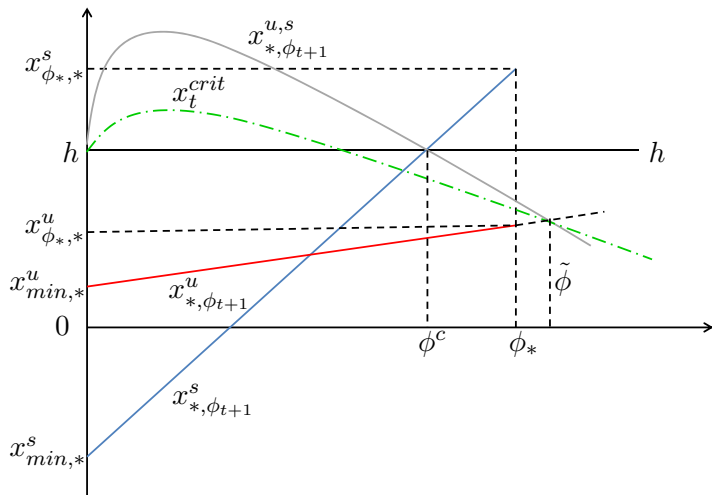
- Households with  $x_t^j < h$  wish to invest in human capital, if  $u_{t+1}^{u,s} \geq u_{t+1}^u \rightarrow y_{t+1}^{u,s} \geq y_{t+1}^u$
- $u_{t+1}^{u,s} = y_{t+1}^u$  implies a minimum level of inherited wealth necessary to become a skilled worker,  $x_t^j = x_t^{crit}$

$$x_t^{crit} = \frac{1}{i_{t+1} - \bar{r}} \left[ (1 - \tau)w^u(1 + \bar{r}) + h(1 + i_{t+1}) - \phi_{t+1}(w^s - w^u) \right] \quad (16)$$

# Dynamics and (conditional) steady states

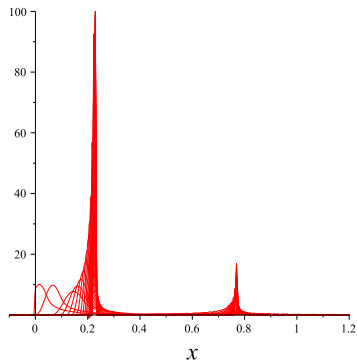
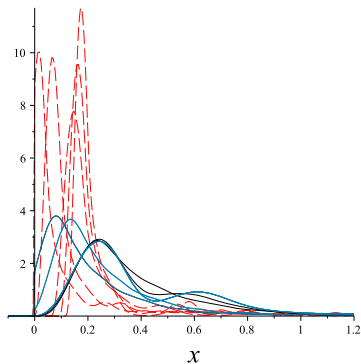


# The evolution of conditional steady states



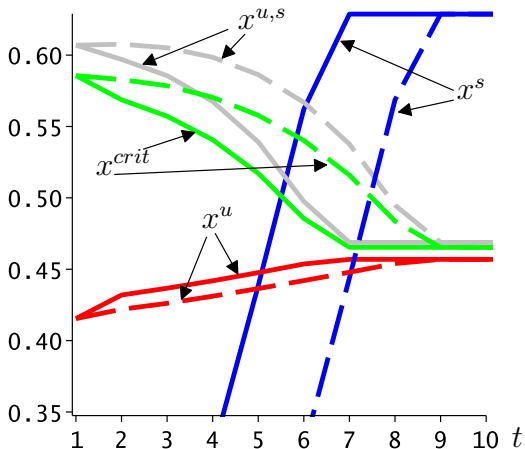
- change in  $\tau$ :
  - benefits both population groups, if the marginal gain in life expectancy  $>$  marginal income loss
  - the marginal gain of the skilled is larger
  
- change in  $\nu$ 
  - benefits both population groups
  - benefits the skilled by more than the unskilled population group

# The evolution of the distribution of wealth



# Higher initial inequality

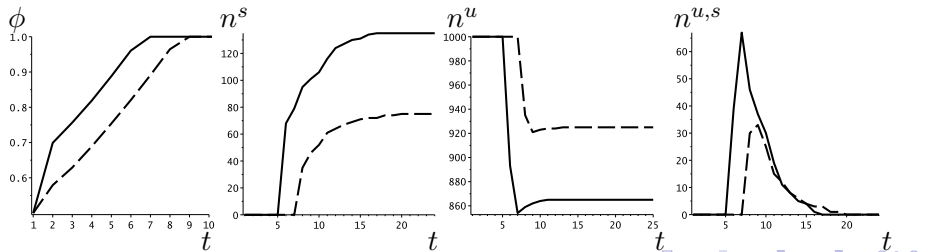
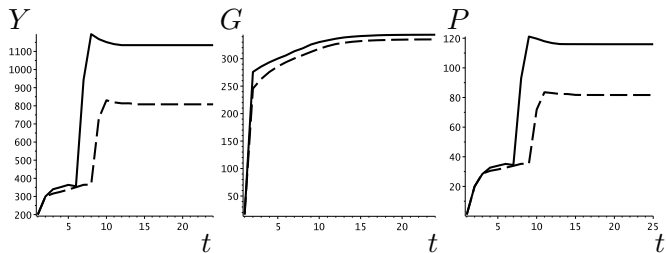
low inequality: solid; high inequality: dashed





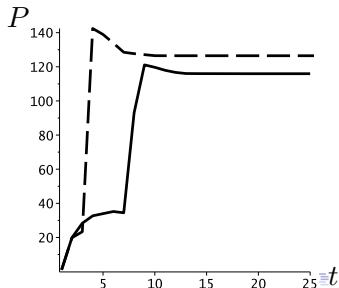
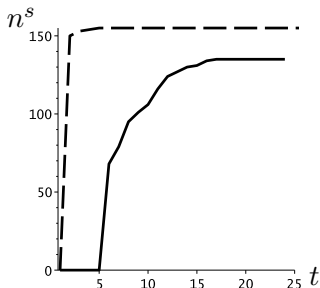
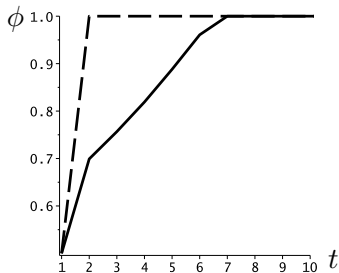
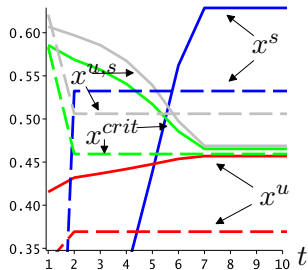
# Higher initial inequality

low inequality: solid; high inequality: dashed



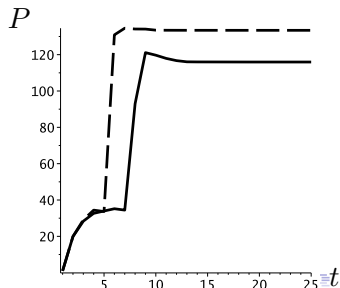
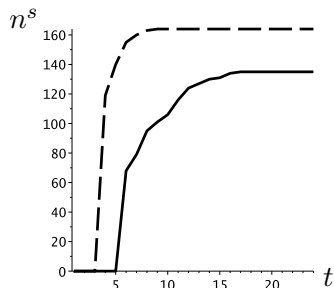
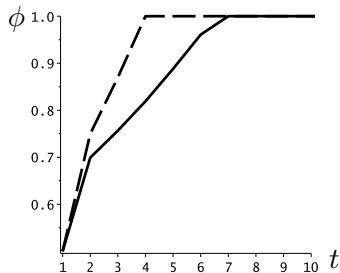
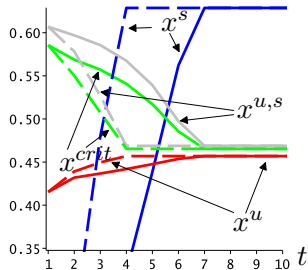
# Increase in $\tau$

low  $\tau$ : solid; high  $\tau$ : dashed



# Increase in $\nu$

low  $\nu$ : solid; high  $\nu$ : dashed



# Summary and Outlook

- Endogenous take-off in terms of human capital accumulation
  - Higher initial inequality delays the take-off, since the tax base is reduced
- higher inequality reduces the effectiveness of a given set of policy parameters in terms of health and abatement expenditures shares
- An increase in the share of public health expenditures seems to be advantageous since it leaves disposable incomes unaffected but increases tax revenues
  - Next steps: endogenous policies and asymmetric effects of pollution on skilled and unskilled households