

# Aggregate-level measures and methods in contemporary fertility research

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Workshop “Measurements and Methods in Demography”

Berlin, 16 October 2009



# INTRODUCTION

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Low fertility in Europe: How to measure it?

**MISMATCH:** Advances and possibilities in fertility measurement not matched with the actual data availability

**DEMOGRAPHIC DIMENSIONS** of analyses:

- Period (years, months) vs. Cohort (birth & parity cohorts)
- Tempo vs. Quantum
- Birth order, age of mother, duration since previous birth

More factors can be added: region, multiple births, men's fertility, education level, country of origin, partnership status

**PRACTICE:** it (almost) all comes down to the period *Total Fertility Rate (TFR)*

# The TFR dominating fertility analysis in the post-WWII era

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- Simple computation: sum of age-specific rates
- ‘Synthetic cohort’ concept, intuitive interpretation (*‘children per woman’*)
- Updated annually (or more often), long time series available for all developed countries

## Alternatives seemingly less ‘attractive’:

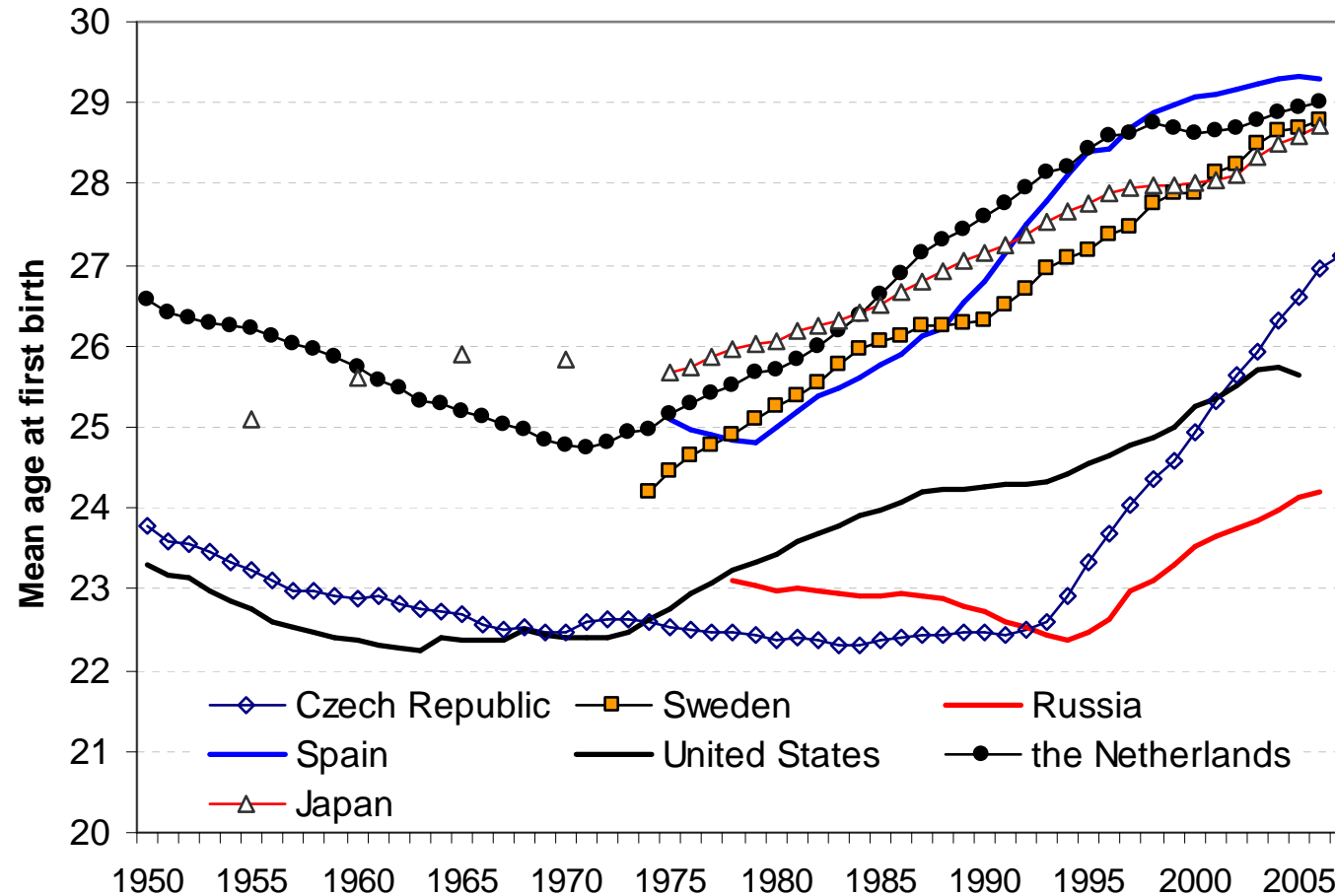
- Long ‘waiting time’ for cohort fertility series
- Missing exposure population in parity-specific analysis
- Other indicators available only for limited number of countries & periods
- Other indexes often less easily understandable or more difficult to construct

## What's wrong with the period TFR?

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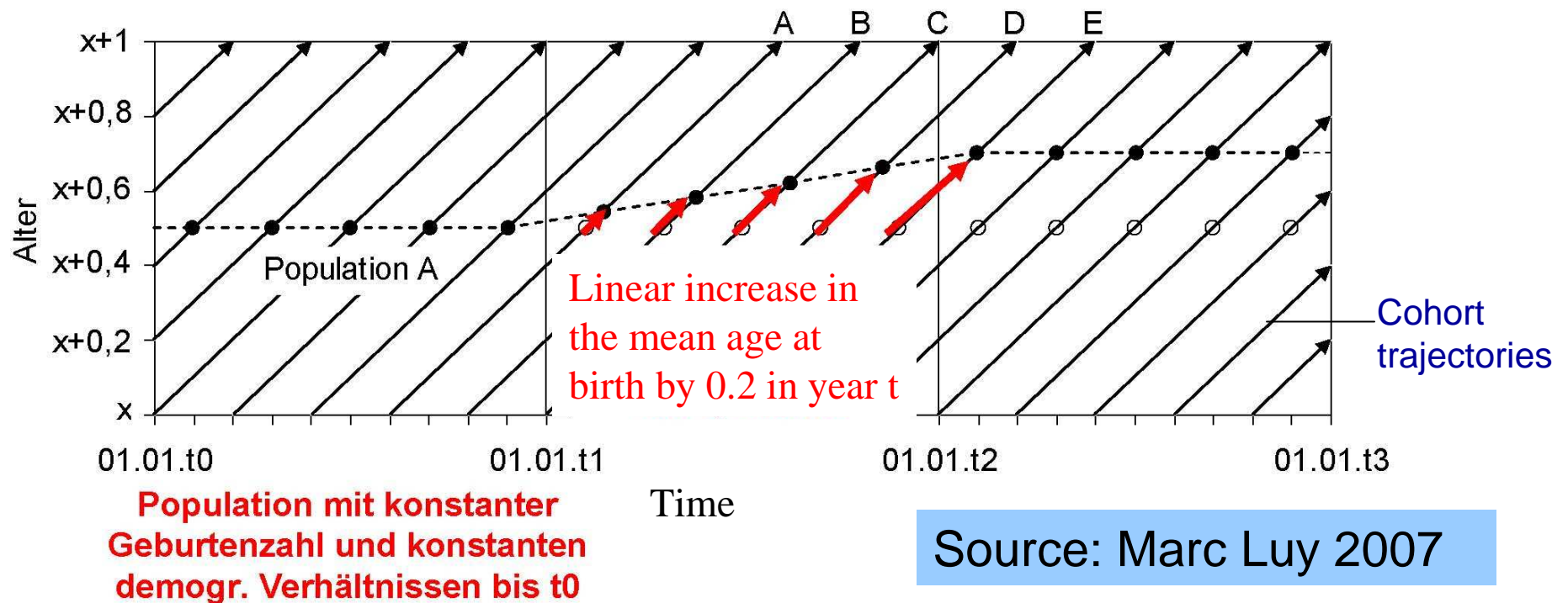
- Controls for some 'key' factors (age & population size), but not for others (parity, duration since the last birth, tempo effects)
- Assumes that children can be born all at once; even women with 3 children are 'at risk' of having first child
- Strongly affected by 'tempo effects' (postponement or advancement of births)
- The 'children-per woman' interpretation is potentially misleading
- Can give incorrect policy messages

# Why timing matters?



*The 'postponement transition'* (Kohler-Billari-Ortega 2002):  
Mean age of mothers at first birth in Europe, US and Japan

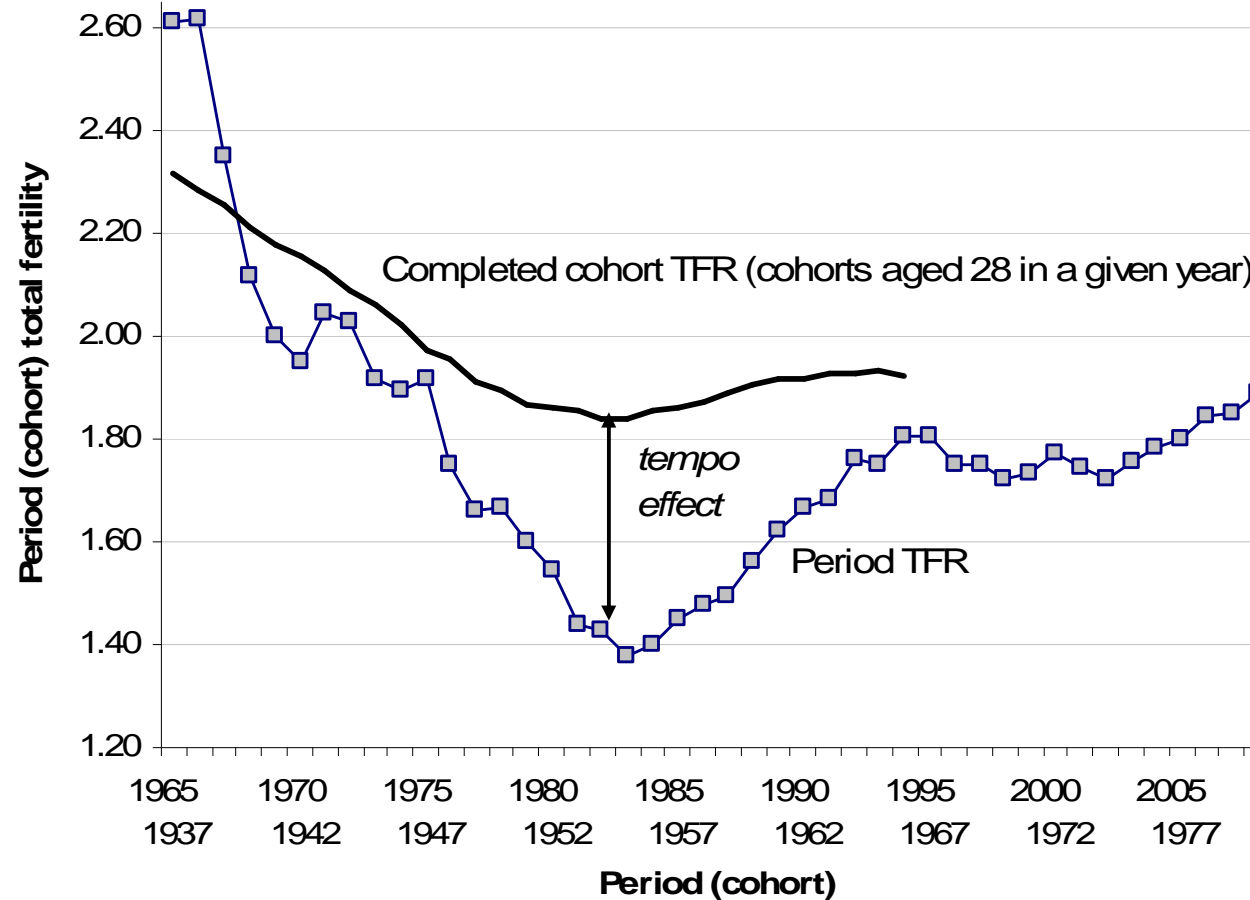
# Tempo effect and the distortions in the total fertility rate: an illustration



*Tempo effects not just minor disturbances: they may be strong and prevail over long periods of time*

# Tempo effects: long-term distortion in the period TFR

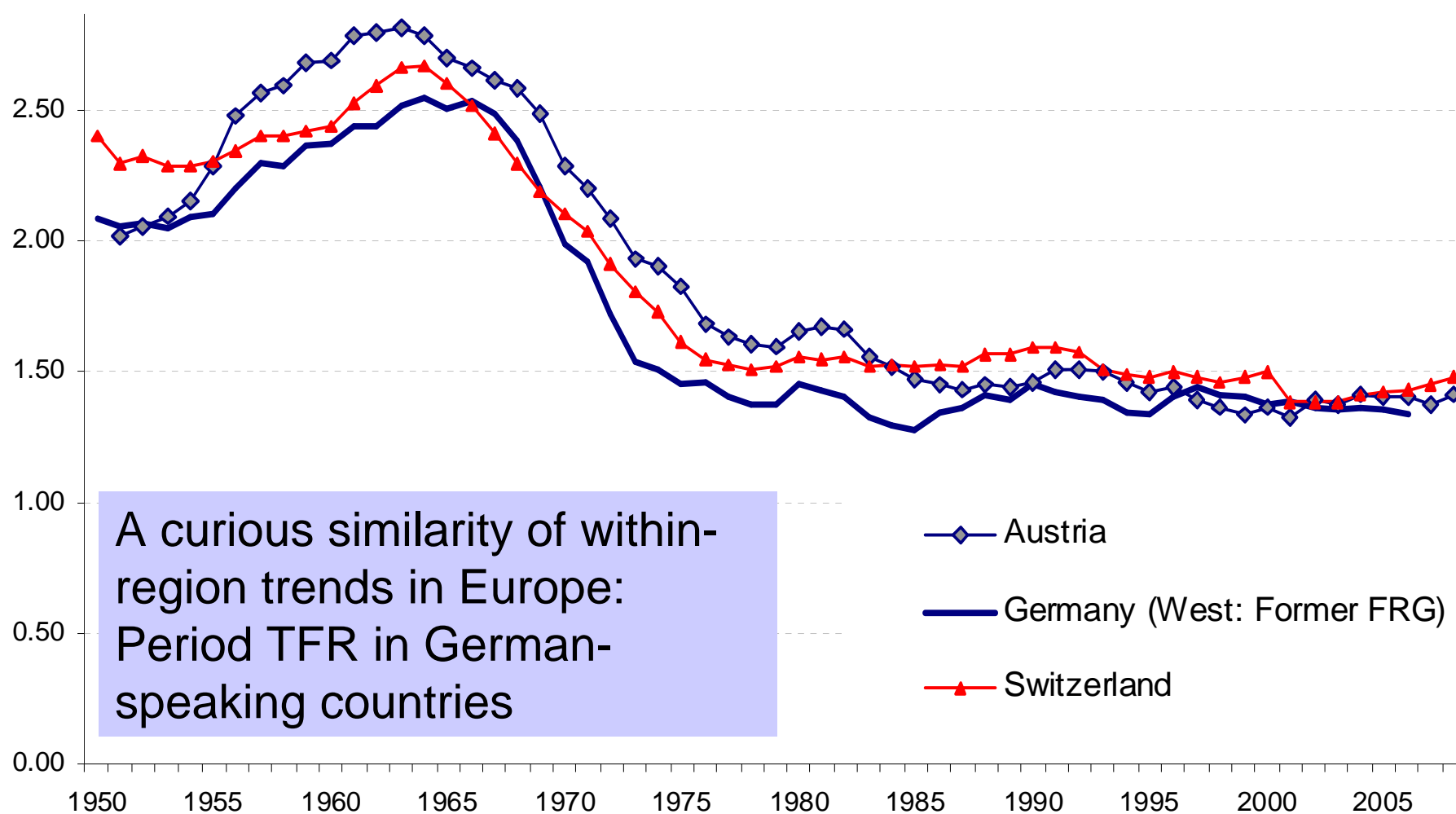
Period TFR (1970-2008) and completed cohort TFR (1942-1964) in Denmark



Data sources: Council of Europe (2006), and own computations from EUROSTAT (2006-9)

# Should period TFR be 'dumped'?

Not necessarily & not always: It (still) often provides useful & readily available information



# AGENDA

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‘Mainstream’ measures and available alternatives: Issues, examples and illustrations

- Cohort analysis: No troubles with the timing?
- Period analysis: A wild array of indicators
  - Parity dimension, fertility tables
  - Tempo-adjusted measures
- Parity cohorts: Bridging period and cohort analysis?
- Emerging issue: How to bring migration in the analysis?

Illustrations: Low and ‘lowest-low’ fertility in Austria and Europe

# 1) COHORT ANALYSIS: No tempo distortions

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## BIRTH COHORTS:

- ‘Completed’ cohort TFR (*CTFR*): no tempo effects
- No interpretation ambiguity: *CTFR* = real number of children per woman
- Some measurement difficulties: cumulating cohort fertility over long periods of time vs. children ever born
- Easy division by birth order:

*CTFR* = sum of order-specific *CTFR<sub>i</sub>*

*Parity Progression Ratios:  $PPR_{i,i+1} = CTFR_{i+1} / CTFR_i$*

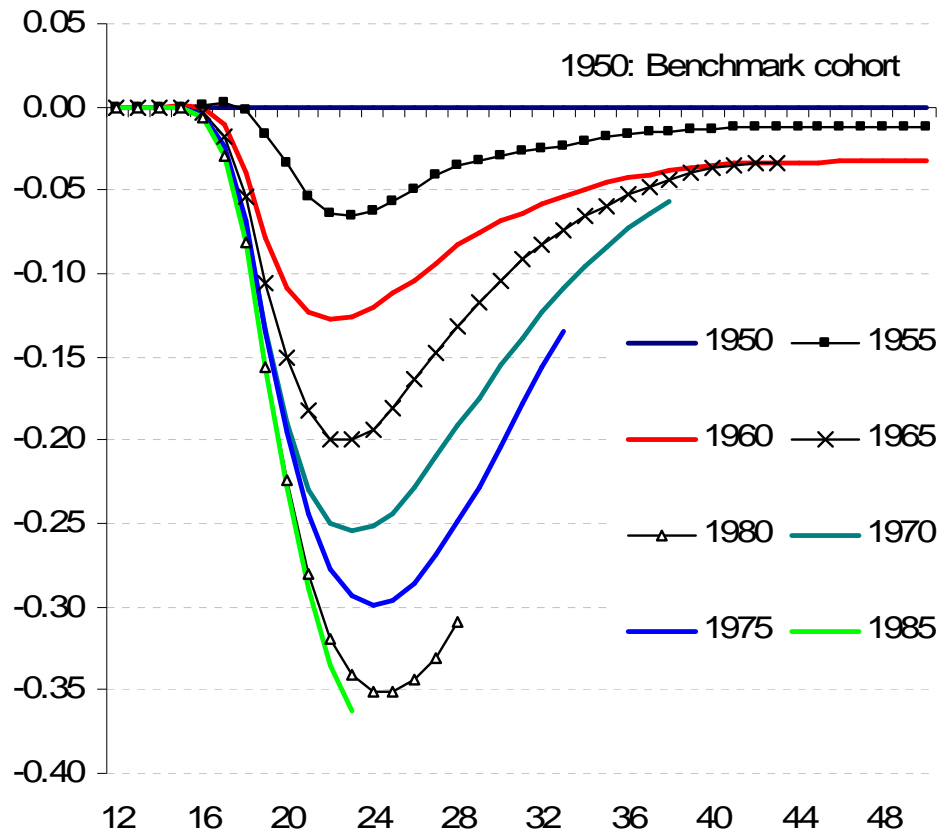
- BUT: ‘long waiting time’ (age 40 at least...)

# Important issues in COHORT ANALYSIS

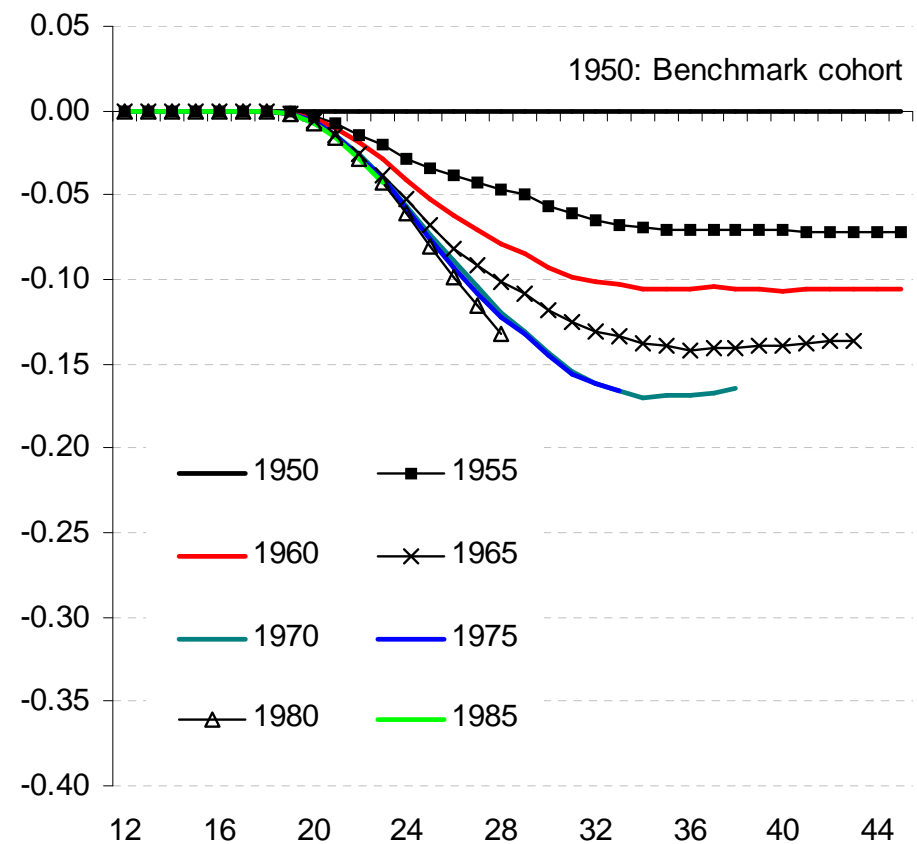
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- 1) Analysing patterns of cohort 'postponement' and 'recuperation': Examples from Austria  
(work with K. Zeman, T. Frejka, R. Lesthaeghe)

# Cohort 'postponement' and 'recuperation': Age-specific 'deficits' related to one benchmark cohort

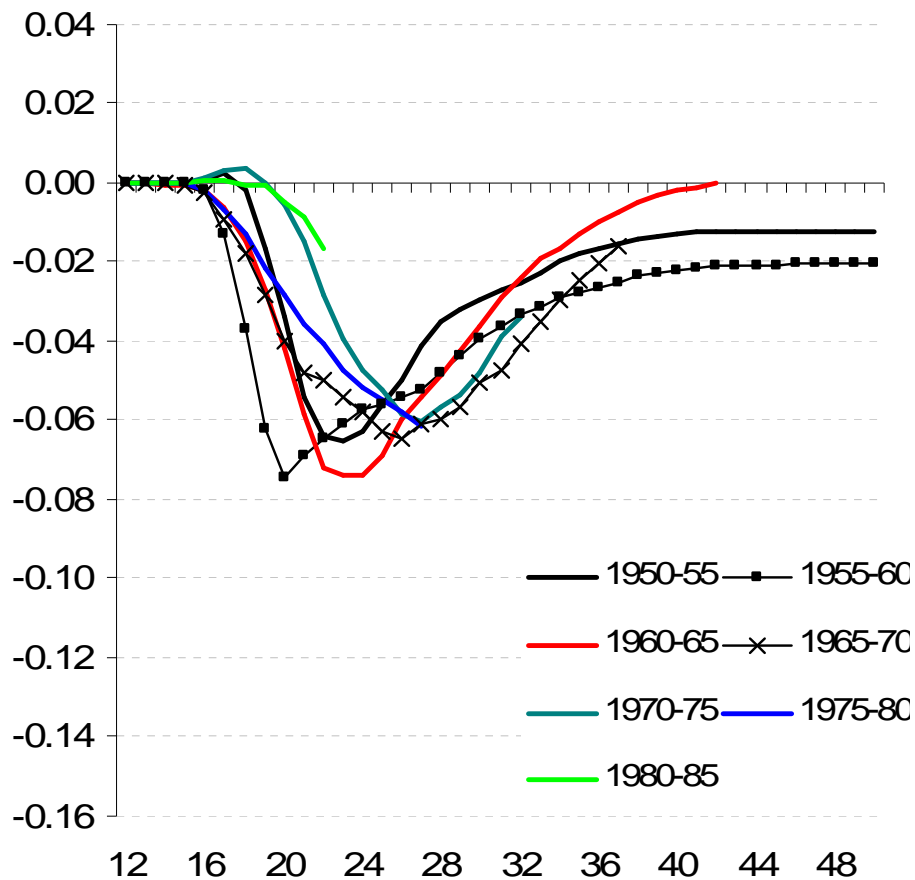


First births

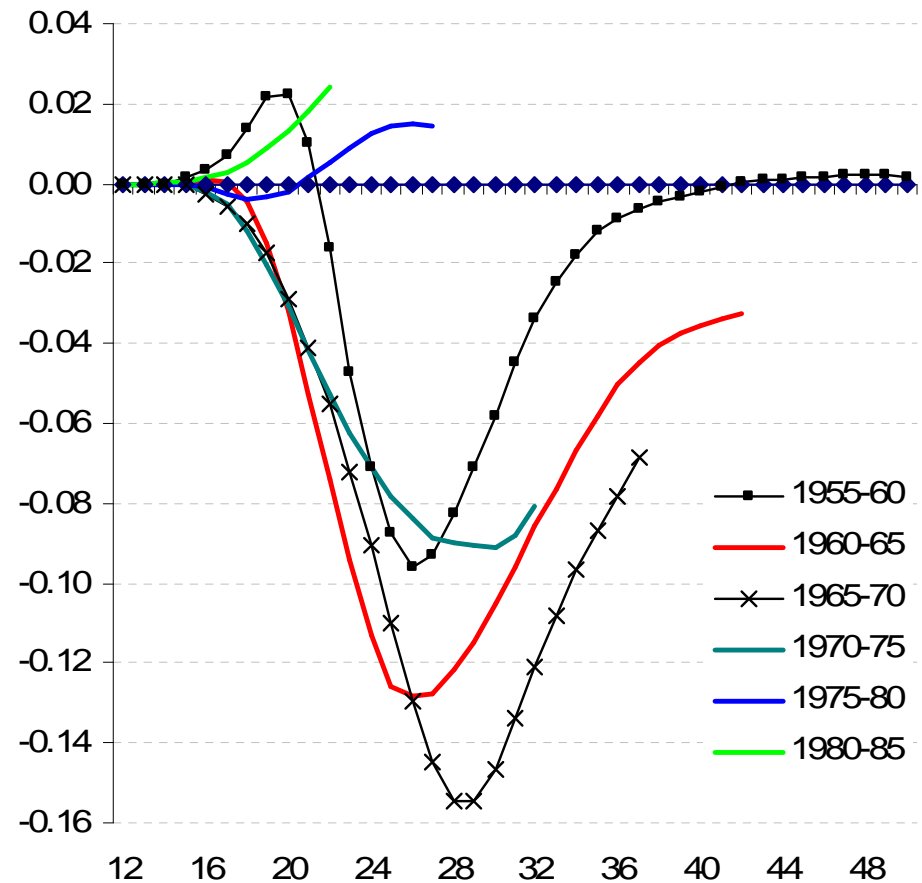


Third+ births

# Cohort 'postponement' and 'recuperation' - Moving benchmark: Age-specific 'deficits' related to the last previous cohort

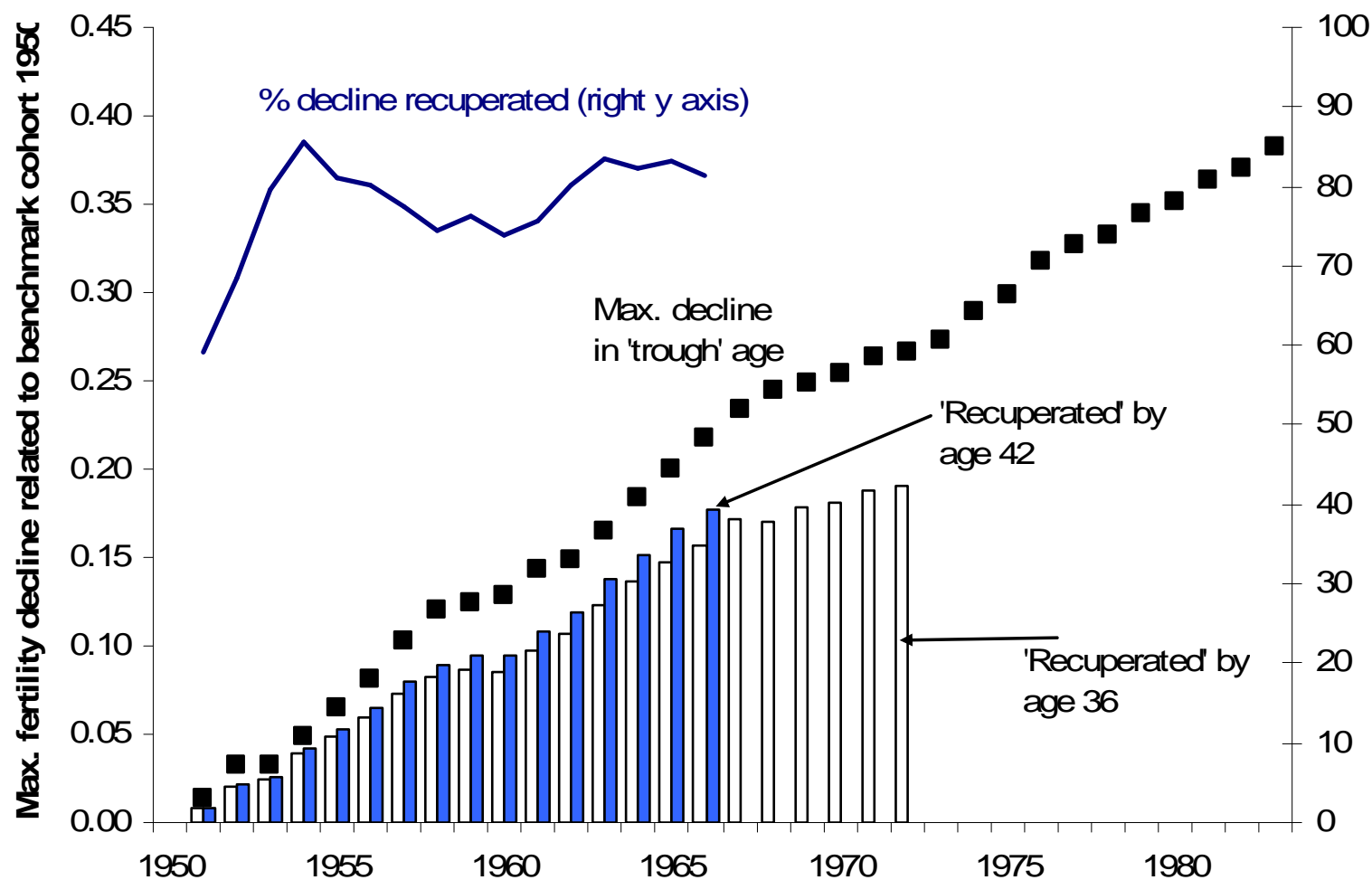


AUSTRIA: First births



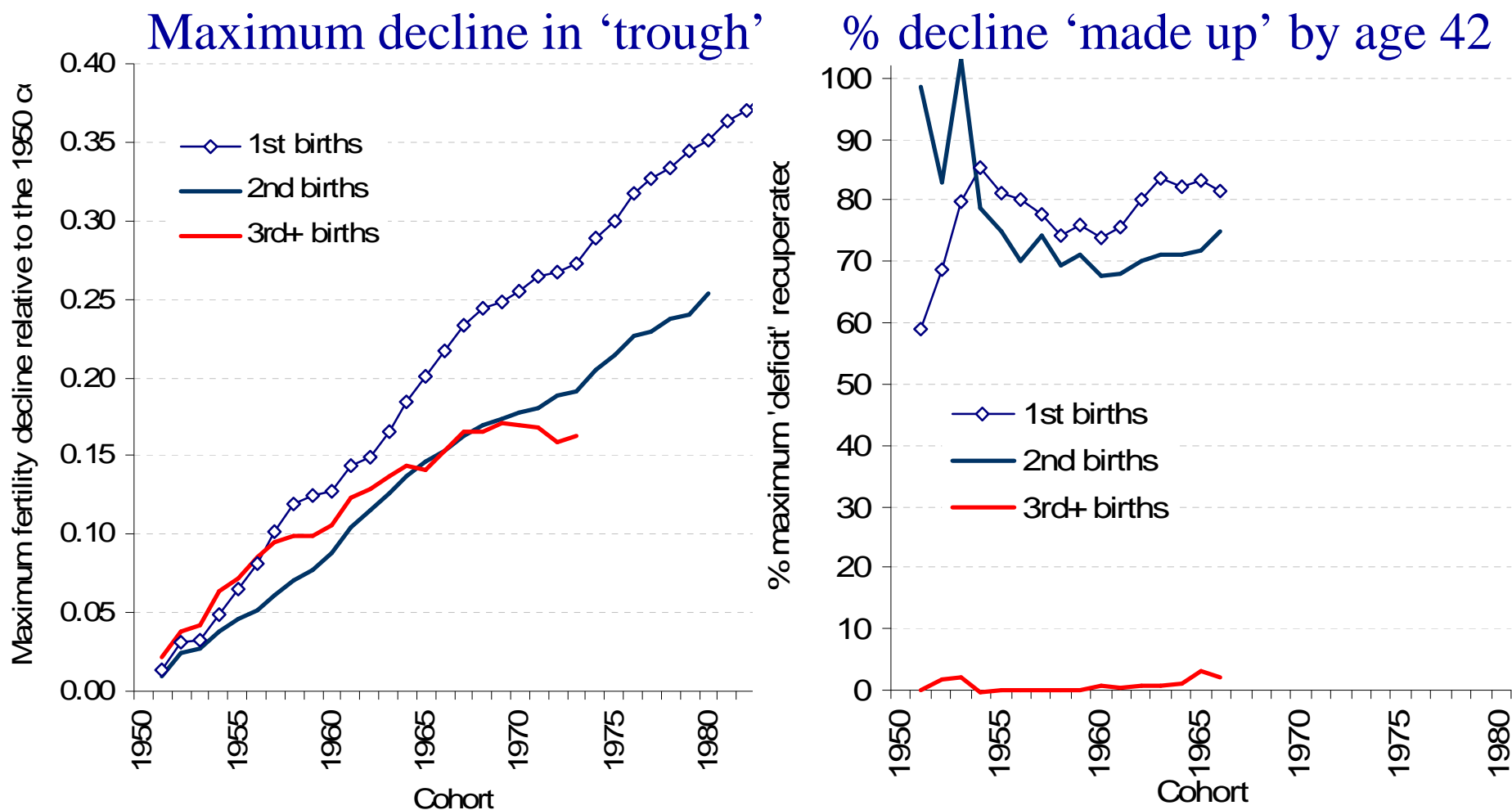
SPAIN: First births

## Cohort 'postponement' and 'recuperation': Summary analysis related to the 'benchmark cohort' initiating postponement



AUSTRIA: First births; cohorts 1950-83 (benchmark cohort 1950)

## Cohort 'postponement' and 'recuperation': Summary analysis related to the 'benchmark cohort' initiating postponement



AUSTRIA: Order-specific differences in delay and 'recovery'

# Important issues in COHORT ANALYSIS

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## 2) Projecting completed fertility of cohorts in reproductive ages

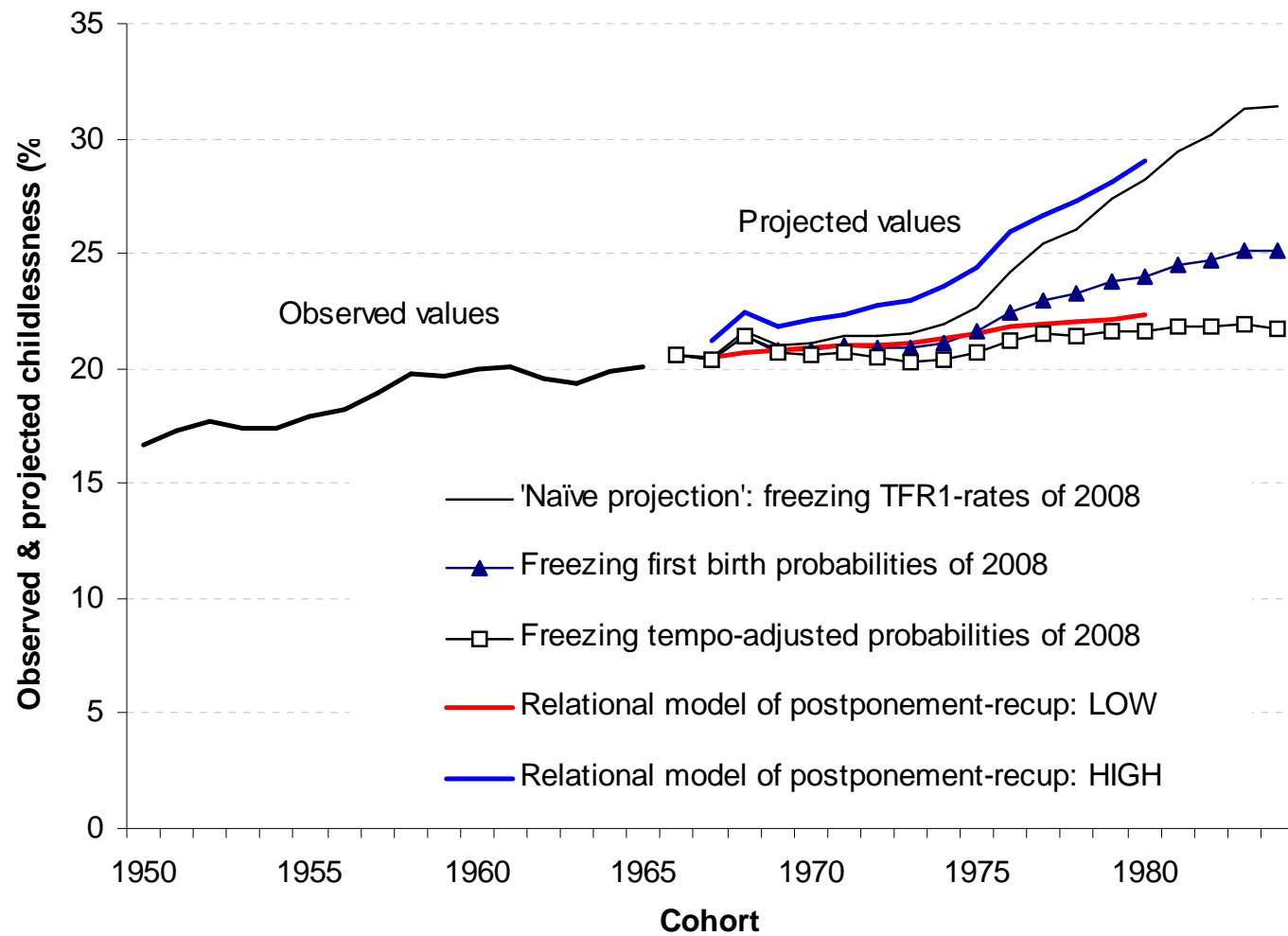
### Different approaches:

- Combining cohort fertility up to date with most recent period rates ('freezing' most recent rates)
- Completing most recent cohort fertility trajectories: trends analyses, regression models...
- Using model fertility schedules

### Key to realistic projections:

- Separate fertility trajectories by birth order
- Take timing shift ('recuperation') into account

# Cohort fertility projections: Childlessness in Austria



## 2) PERIOD analysis: Beyond the TFR

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- How to measure the 'underlying' period fertility levels?
  - *No unambiguous alternative to the TFR*

Two major alternatives:

- 1) Shift to the more sophisticated, **parity-specific measures** (indicators controlling for age & parity or parity & duration since the previous birth); *also distorted by tempo effects!*
- 2) **Adjustment approach:** Attempts to correct the period measures for tempo distortions (e.g., Bongaarts-Feeney (1998), Kohler-Ortega (2002)); *not universally accepted!*

# PERIOD analysis: Parity-specific measures

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## Controlling for the parity distribution of the female population

- Takes away one obvious distortion in the TFR
- **Data hurdle:** Many countries lacking data on births by 'true' birth order and parity distribution (often birth order within marriage!)

Important distinction: non-exposure rates by birth order (type 2 rates, incidence rates) vs. **parity-specific rates** (type 1 rates: occurrence-exposure rates, probabilities, 'conditional' rates)

Example: 1<sup>st</sup> births at age 27

Type 1 rates (exposure): first births related to childless women only:

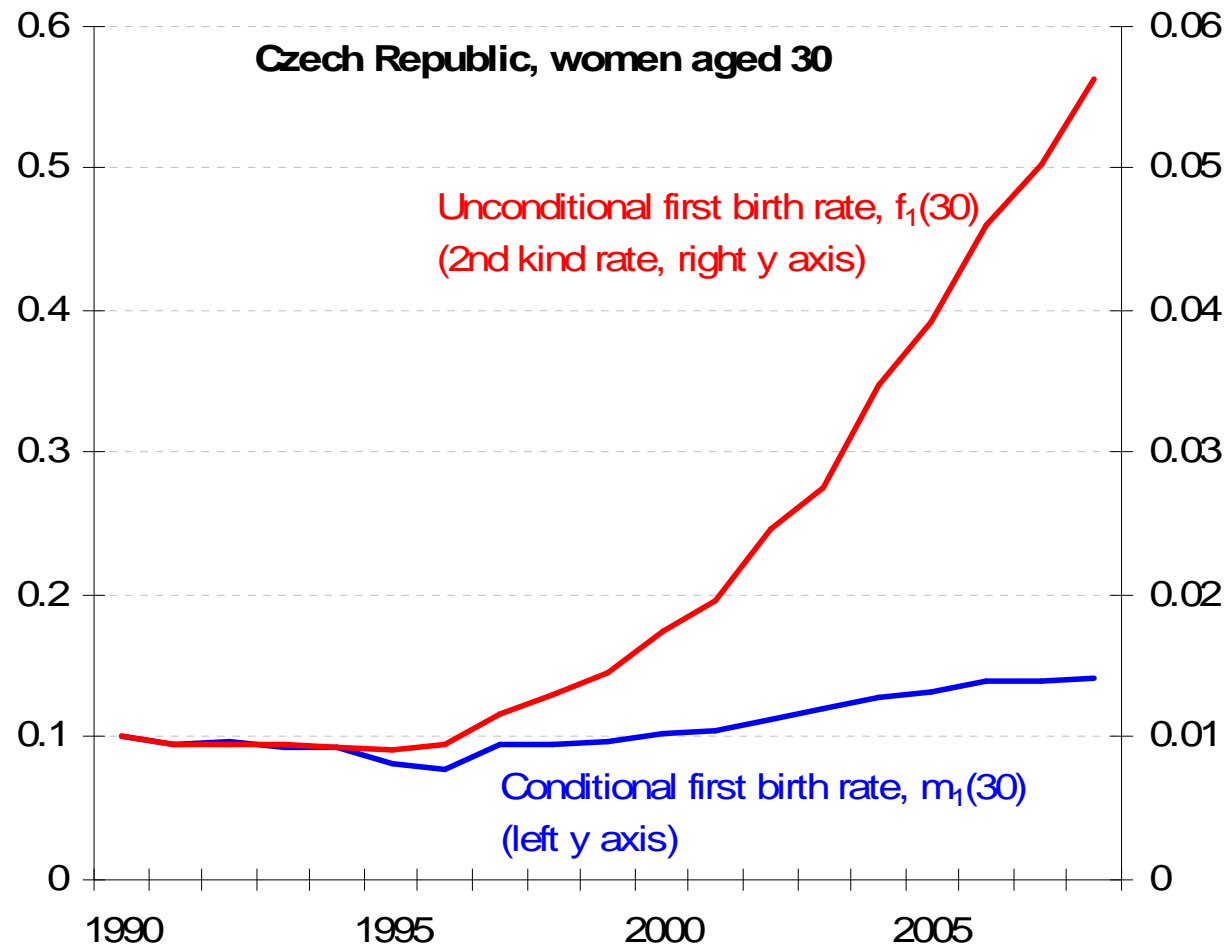
$$m_{i=1}(27) = B_{i=1}(27) / P^F_{i=0}(27)$$

Type-2 rates (non-exposure, TFR-type rates): first births related to all women of a given age:  $f_{i=1}(27) = B_{i=1}(27) / P^F(27)$

$i$  = parity of the woman or birth order of the child

# PERIOD analysis: Parity-specific measures

Controlling for parity may give very different insights



First birth rates change at age 30, Czech Republic 1995-2008:

Unconditional rates ( $f_1(30)$ ):  
Factor 6.2

Parity-specific rates,  $m_1(30)$ :  
Factor 1.7 (+74%)

% childless: 13% in 1995, 43% in 2008

# PERIOD analysis: Parity-specific measures

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## Parity-specific indicators: Layers of analysis

### Two major dimensions: Age & duration since the previous birth

- Time elapsed since the previous birth more important than age for women with 1+ children (Ní Bhrolcháin 1992) (common assumption in multiplicative regression models)
- Duration (birth interval) analysis explored further in the next talk
- Schedules of age-parity specific rates can be used to construct multistate (increment-decrement) **fertility tables**

# PERIOD analysis: Fertility tables by age & parity

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Period fertility tables (FT): model childbearing history of synthetic cohorts of women

- Huge analytical potential, many functions

Key inputs of FT controlling for age & parity: age-parity distribution of women, live births by birth order and age

Mortality tables: timing = life expectancy main output;

Fertility tables: quantum (fertility index, conditional fertility rates / probabilities)

Selected functions:

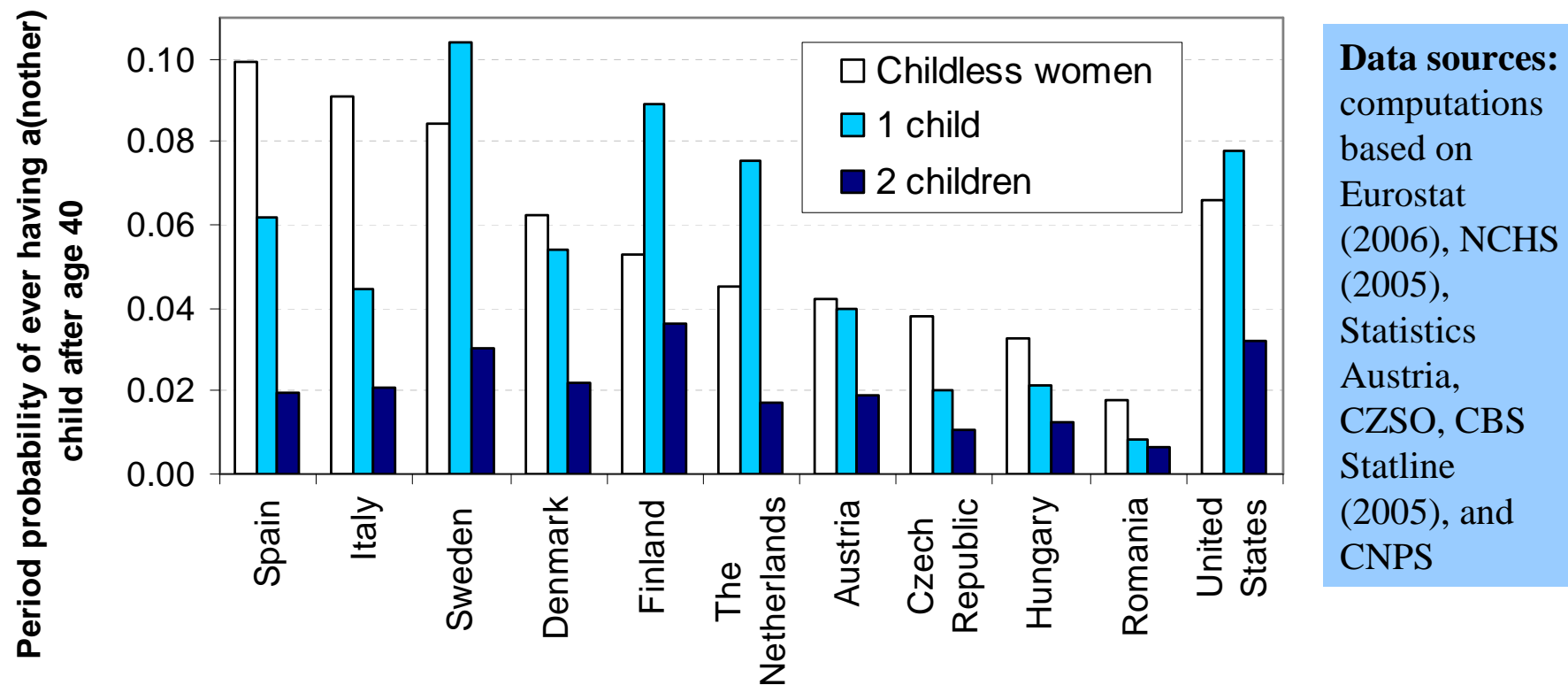
$q_i(x,y)$ : probability of having an  $i$ -th birth in age interval  $[x, y]$

$Q_i(x)$ : 'Lifetime' probability of having an  $i$ -th birth when at parity  $i-1$  at age  $x$

$PATFR_i$ : Period fertility index for birth order  $i$  (Ralu and Toulemon 1994)

# Period fertility tables & indicators: Illustrations

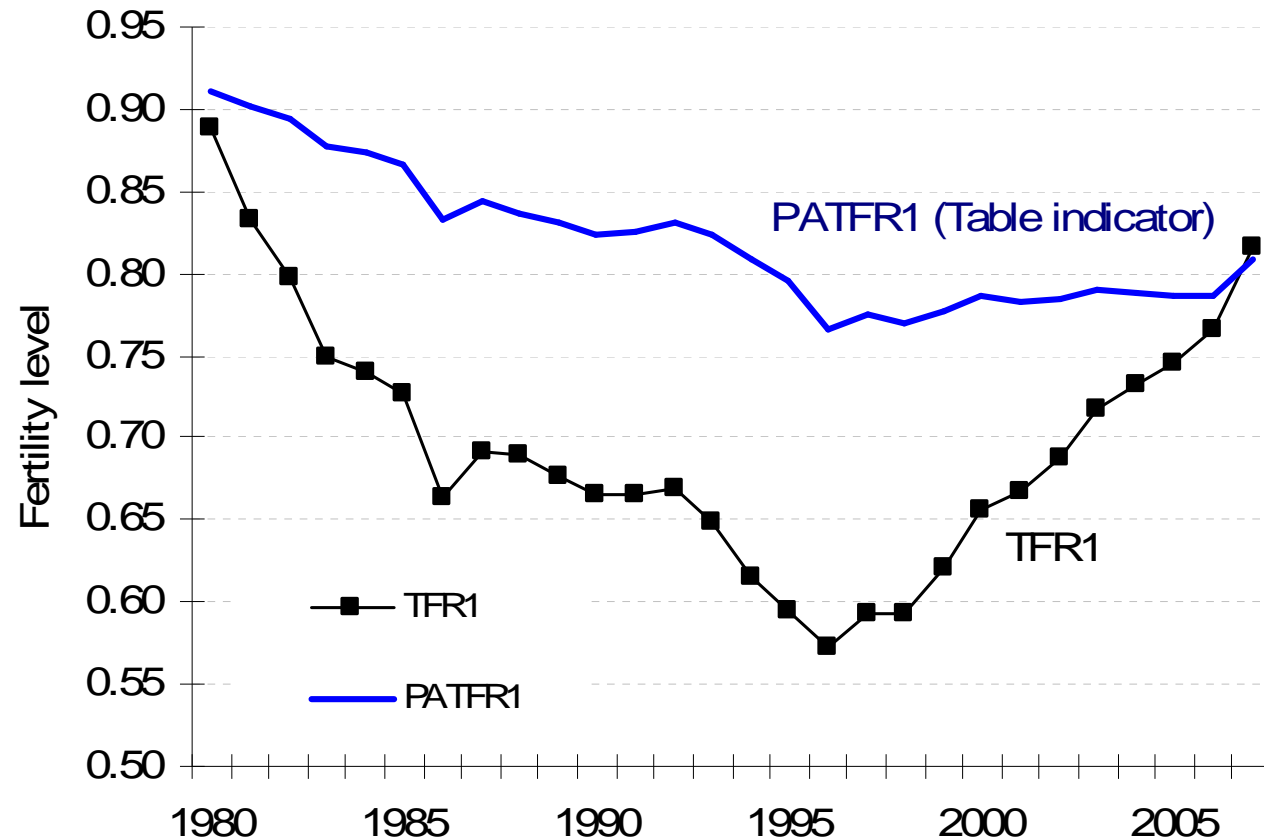
## Example 1: Parity-specific fertility differences at advanced reproductive ages



$Q_i(40)$ : Conditional ('Lifetime') probability of having another child by parity at age 40 (women in selected countries, ca. 2004)

# Period fertility tables & indicators: Illustrations

## Example 2: A sharp increase in first birth rates in Spain



1996-2007:

PATFR1:

+6%

TFR1

+43%

# Period fertility: Tempo adjustment

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## Tempo effects in period fertility rates: Major issues

- Is tempo effect a distortion? Or an integral part of period fertility indicators?
- Can we distinguish 'tempo' and 'quantum' effects in period rates?
- Should we try to filter out tempo effect? (Redefinition of period indicators and rates in a 'synthetic cohort': from 'current rates' to 'current conditions' (Bongaarts 2009))
- (Tempo)-Adjusted measures are just trying that!

# Period fertility: Tempo adjustment

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## Tempo effects: Adjustment explosion

The idea of adjusting period fertility stems from [Ryder's 'translation'](#) of cohort rates to period rates and back

- [Bongaarts and Feeney \(1998; BF\)](#): adjusting order-specific  $TFR_i$  (Before them, [Murphy \(1994\)](#) tried with the overall TFR)
- [Kohler and Philipov \(2001\)](#): age-specific adjustments in unconditional rates by birth order,  $fi(x)$
- [Kohler and Ortega \(2002\)](#): age-specific adjustments in parity-specific rates ( $PATFR_i$ )
- [Other attempts](#): [Yamaguchi-Beppu 2004](#), [Schoen \(2004\)](#): Average Cohort Fertility...  
BF clearly most successful

# Period fertility: Tempo adjustment

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The successful march of the BF adjustment

Methodological superiority? NO: problematic assumptions; critical discussion about the usefulness of BF approach

**BUT:** Data availability, easy computation, easy understanding, and... BF came first!

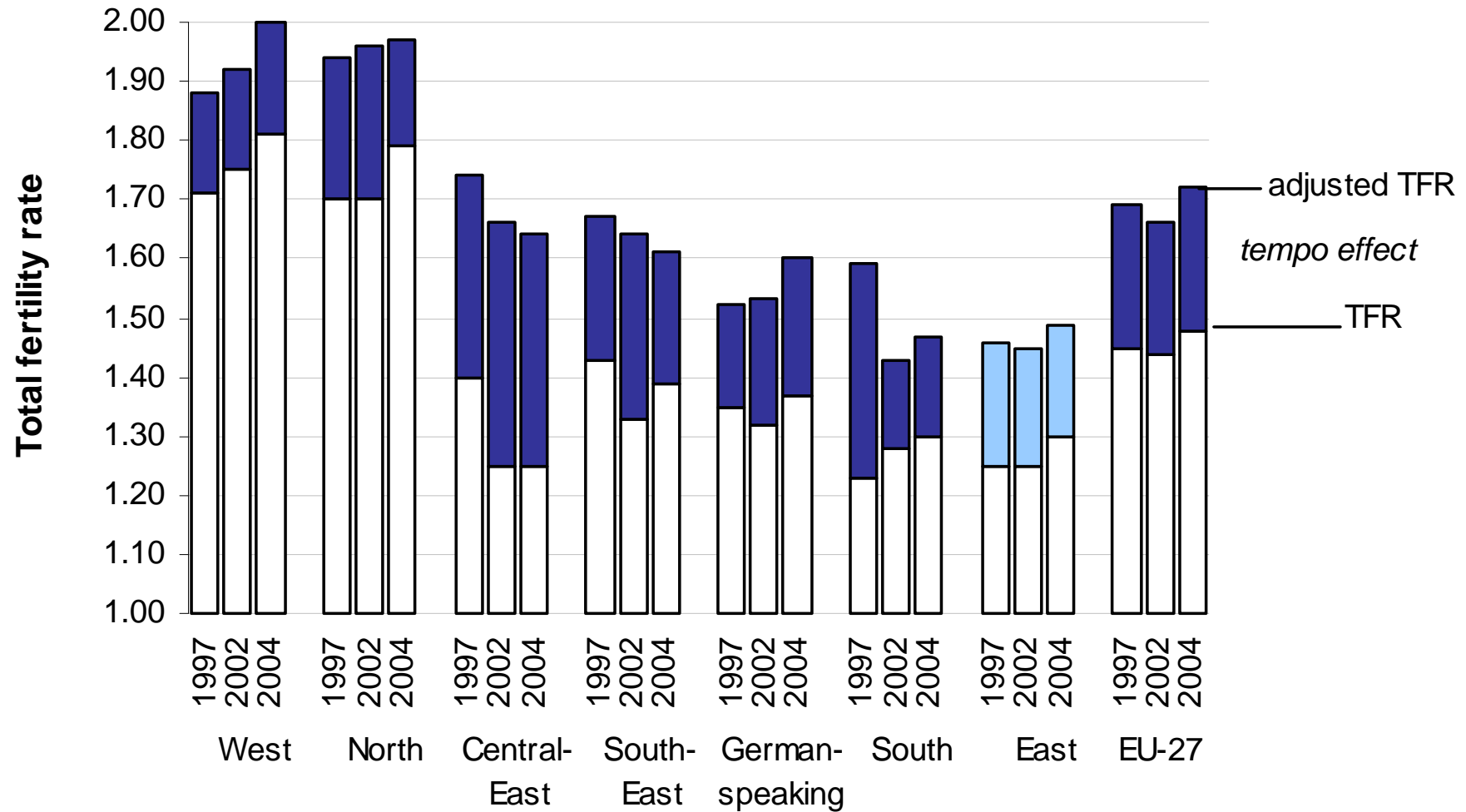
BF adjustment ideas now catching up in **mortality analysis**  
(= adjusting tempo, not quantum indicators)

Tempo-adjusted TFR:

$$adjTFR_i = TFR_i / (1 - ri(t)); \quad adjTFR = \sum adjTFR_i$$

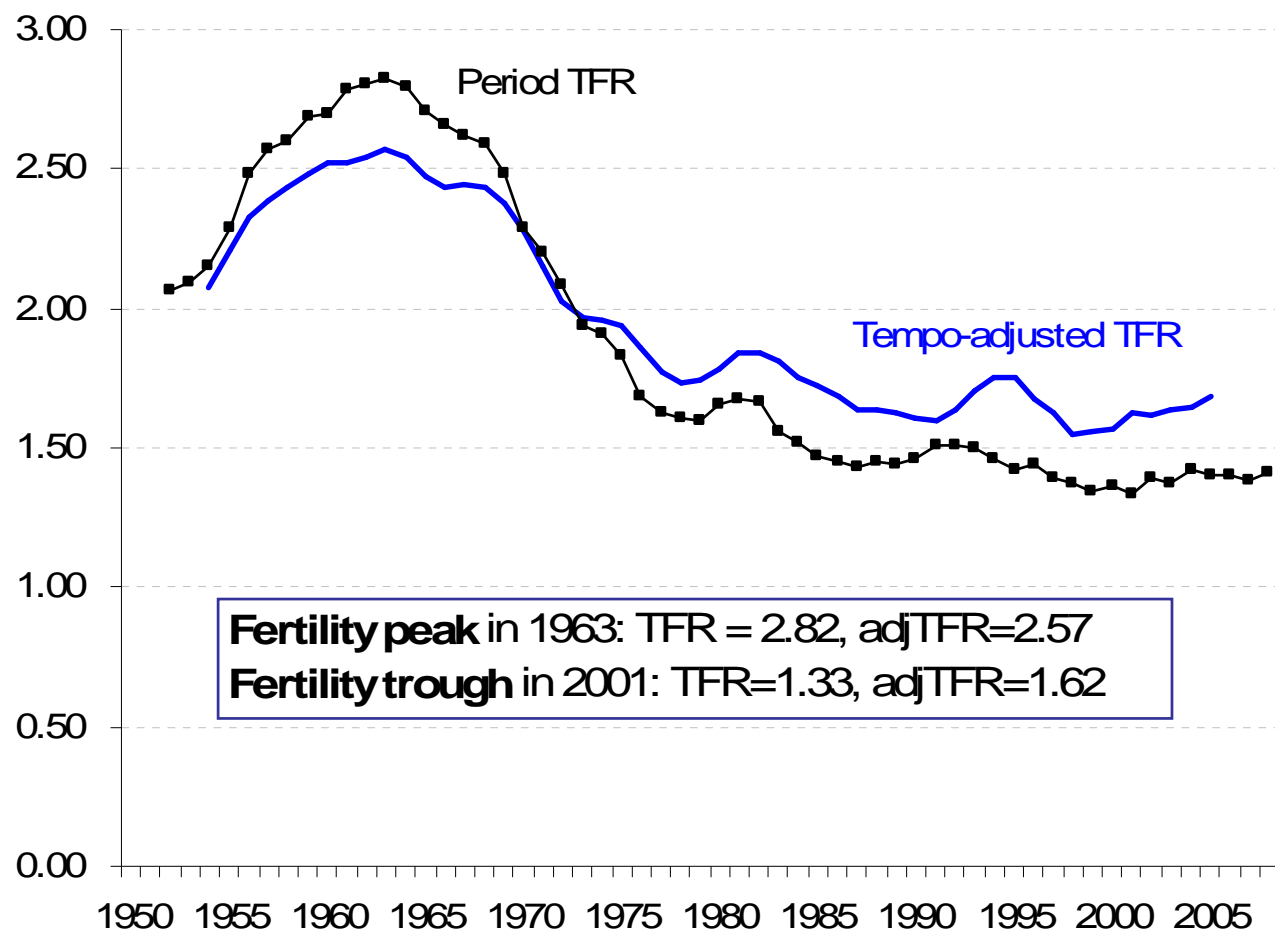
Where  $ri(t)$  is the change in the mean age at childbearing at birth order  $i$ :  $ri(t) = MAC_i(t+1) - MAC_i(t-1) / 2$

# Period fertility contrasts in Europe: A view with the adjusted TFR



Sources: Sobotka 2004, VID 2006 and 2008

# Post-war period fertility in Austria: TFR vs. adjTFR



**Fertility peak** in 1963: TFR = 2.82, adjTFR=2.57  
**Fertility trough** in 2001: TFR=1.33, adjTFR=1.62

Baby booms and busts in part fuelled by tempo effects (advancement vs. postponement of births)

Sources: Statistics Austria, Eurostat, Geburtenbarometer, Computations by T. Sobotka & Anna Stastna

### 3) Parity cohorts: Bridging period and cohort analysis?

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**Parity cohort:** A group of women (men) who had an *i-th* child at the same time (year, month); e.g. parity 1 cohort of 2000

**ANALYSIS:** Following their subsequent childbearing

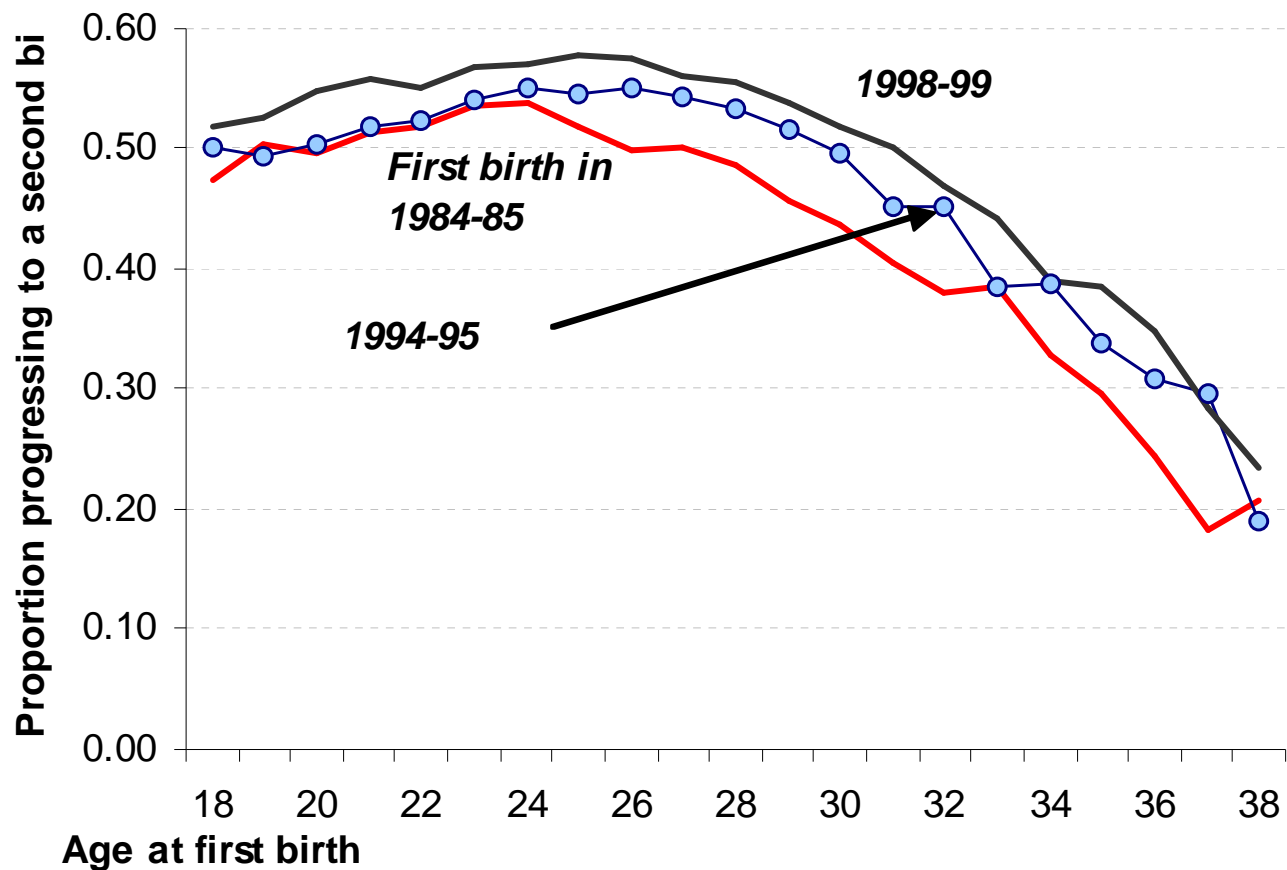
**Tempo:** birth intervals

**Quantum:** parity progression rates (PPRs), cumulative progression after 1 year, 2 years, ....

**Why interesting?**

- cohort analysis, but with a short 'waiting time'
- although birth intervals of 20-30 years occur, most subsequent births within 2-5 years
- stable birth intervals in many countries; high predictability of parity progressions after 5 years of observation

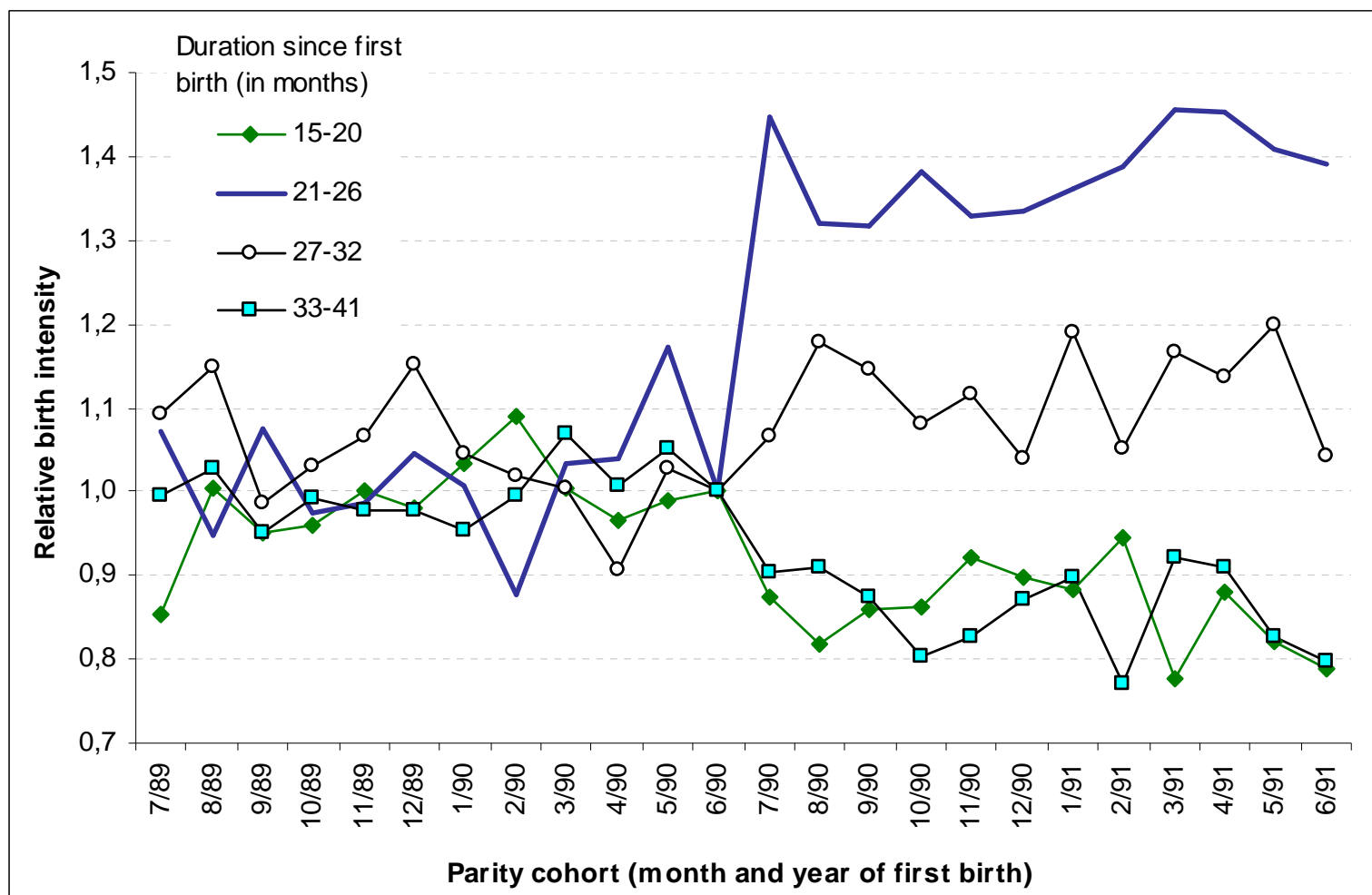
# Parity cohorts: Illustrations



Progression rate to second birth 4 years after the first one, Austria, women having first birth in 1984-1999

# Parity cohorts: Prolongation of parental leave and second births in Austria

Second birth rates by duration since last birth, Parity-1 monthly cohorts (Rates relative to the June 1990 parity 1 cohort)



Source:  
Šťastná  
and  
Sobotka  
2009

## 4) Fertility, migration and population replacement: How to bring migration in the analysis?

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Importance of immigration:

Need to rethink traditional concepts of replacement fertility

Hyrenius (1951): *Reproduction and replacement*

Different measures of 'migratory fertility', replacement rates with migration etc. discussed and developed (Daguet 1995, Calot & Sardon 2001, Smallwood & Chamberlain 2005, Preston 2007, Alho 2008, Ediev 2008....)

Replacement migration may occur even in societies with sustained very low fertility rates (Spain, Switzerland)!

# Replacement migration: PERIOD perspective - an illustration for Austria

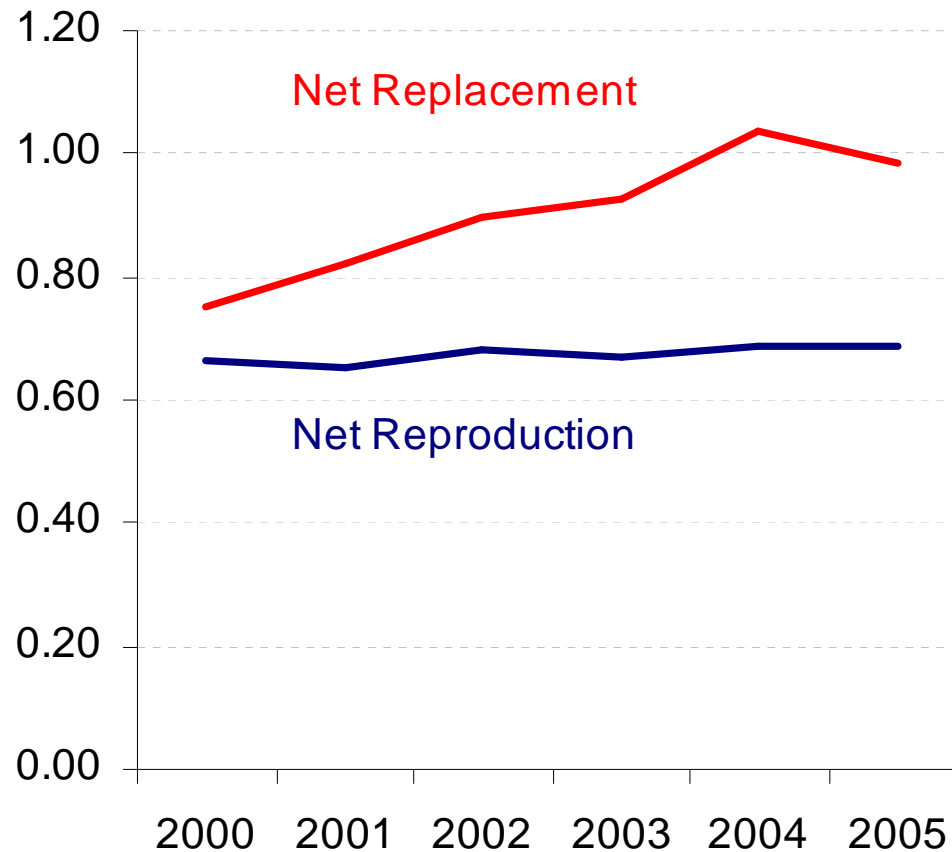
<b>Net reproduction rate in Austria, 2004-2005</b>	
TFR	1.41
survivors at age 30	98971
survivors at age 50	97265
Table number of female children born	68237
<b>Net Reproduction Rate</b>	<b>0.682</b>
Intrinsic rate of population growth	-1.32%

Now, let's expose the initial synthetic cohort of 100,000 baby girls to female net migration rates by age in 2004-2005

<b>Net replacement rate in Austria, 2004-2005</b>	
TFR	1.41
Table population at age 30	151110 (+53%)
Table population at age 50	167323 (+72%)
Table number of female children born	101098 (+48%)
<b>Net Replacement Rate</b>	<b>1.011</b>
Intrinsic rate of population growth	0.04%

# Replacement migration

Net Reproduction and Net Replacement in a period view, Austria, 2000-2005



➤ this analysis underestimates the impact of immigration!

# Replacement migration: COHORT perspective

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Measuring longer impact of immigration:

GRE (=Gross REplacement rate):

tracing changes in the relative cohort size of females from birth on

At birth:  $GRE(t) = GRR(t)$  (*Gross Reproduction Rate*) =  
=  $TFR * (\text{female live births} / \text{all live births})$

At age 30 (final GREF):

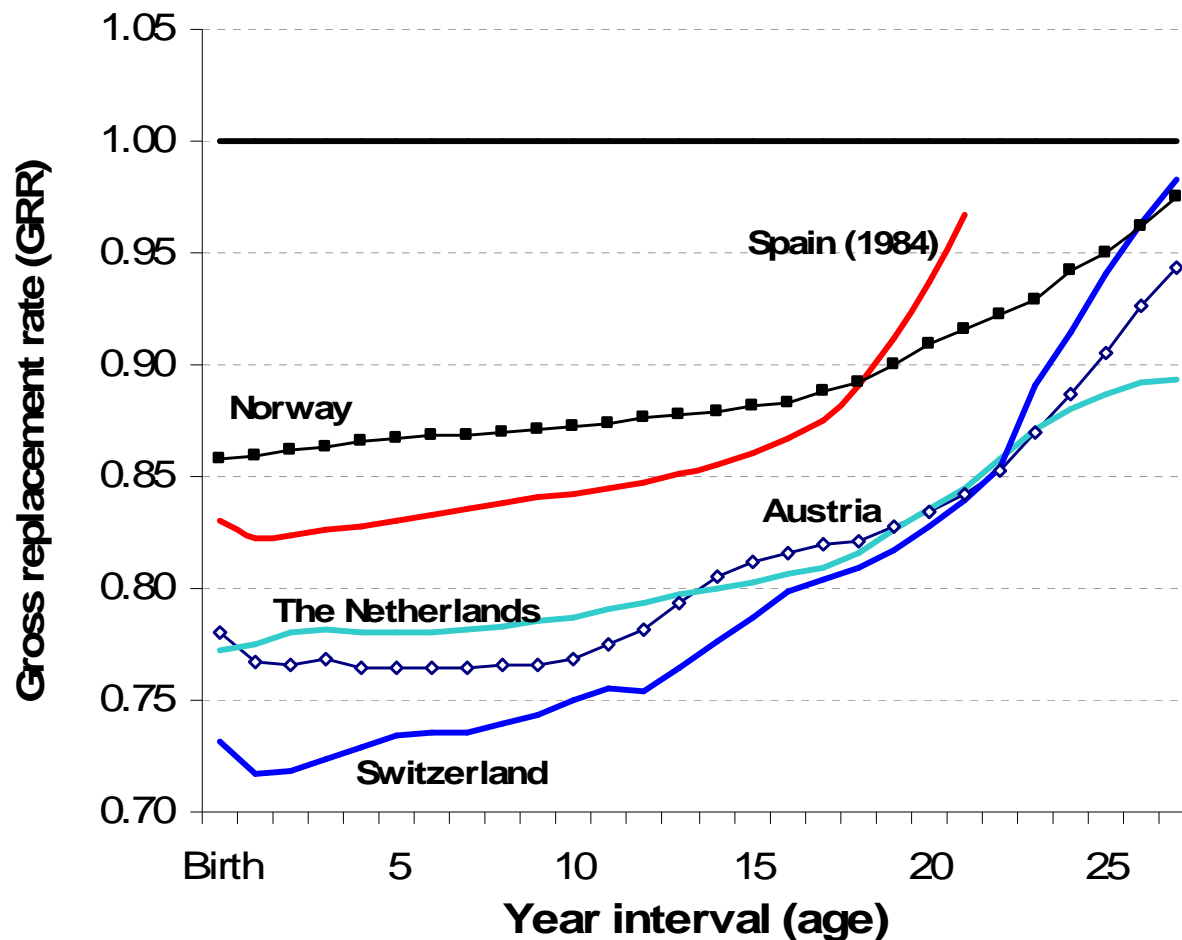
$GREF(t) = PF(t+30)/PF(t) * GRR(t)$

Advantage: Easy computation, accessible data

Interpretation: summarises both the effects of migration and mortality on the relative size of female cohorts before reaching their prime childbearing age

# Replacement migration: Gross Replacement Rate – an illustration

5 countries: GRE for 1978 (1984 for Spain)



*Younger cohorts:  
further decline in  
the GRE at age 0  
and faster  
subsequent  
increase*

Source: Computations in  
Sobotka (2008)

# CONCLUSIONS: Going beyond the period TFR

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Models of period fertility: Discussed indicators are models of behaviour; abstract, hypothetical and loaded with assumptions

TFR somewhere in the middle in the complexity of period measures

- Live births
- Crude birth rate (controlling for population size)
- **Period TFR (controlling for size and age structure)**
- Table PATFR (controlling for size, parity composition and age structure)
- Parity Progression Ratios (controlling for size, parity composition and duration)
- Kohler-Ortega adjusted PATFR Table PATFR (controlling for size, parity composition, tempo effect and age structure)

*Period TFR was a great innovation in 1907, when Kuczynski proposed it at a congress ... in Berlin. Now time to disseminate a range of other measures! (Human Fertility Database)*

# What indicators should be used?

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One does NOT fit all: The choice of fertility measures should be determined by the research question asked (Ní Bhrolcháin 2008)

- Some questions addressing cohort issues (e.g., the gap between intended and achieved family size)
- Some questions pertaining to specific birth orders or age groups: “What portion of ‘postponed’ first births occurred later in life?”
- Some questions concerned about timing: “Did the past economic crises cause a genuine decline in fertility rates or ‘just’ fertility postponement?”

# What indicators should be used?

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## Key issues in low-fertility countries

**Parity matters:** Understanding parity-specific fertility behaviour key for understanding fertility differences and trends across regions (e.g., huge parity differences in cohort postponement & 'recuperation')

**Timing matters:** Tempo effects (mostly due to 'postponement') can lead to wrong interpretations of trends, levels and cross-country differences

- Both also paramount for projection-making, both period & cohort

**Migration matters:** Population change in many countries increasingly driven by migration – how to put migration in the picture?

# What indicators should be used?

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No one indicator of choice, a bouquet of indicators should be published and used in parallel

- Less TFR, especially in comparative & policy-relevant analyses
- Avoid 'children per woman' interpretation in the TFR
- More prominence to duration-specific rates

*We need data, data and ... more data (especially Germany!)*

- Future data & methods important areas:
  - Fertility and migration combined (population replacement)
  - Men's fertility
  - Monitoring of fecundity, infertility, time to conception
  - Partnership and fertility (marriage is obsolete?)
  - Fertility recuperation & determinants

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## Period TFR may give misleading messages

- Fertility rates in Europe higher when other indicators used
- Recent TFR increase largely fuelled by the slowing-down in fertility postponement (Goldstein-Sobotka-Jasilioniene 2009)
- Fertility 'quantum' (levels) often more stable than the 'roller-coaster' TFR suggests

## Limits of the macro-level analysis?

- Detailed and complex indicators pushing the limits of the macro analysis; getting close to individual-level research